

## **STRAIGHT LINES V2.02**

This short program from the field "Vector Algebra" finds for two straight lines

**L<sub>1</sub>:  $s_1 + \lambda \cdot t_1$**  and **L<sub>2</sub>:  $u_2 + \mu \cdot v_2$**

the distance between the lines, the points P1 and P2 of the minimal distance on both lines, the intersection angle  $\alpha$  and checks, whether the lines are parallel or have a common point of intersection. If **v<sub>2</sub>** is entered as **{0,0,0}**, the problem is handled as straight line **L<sub>1</sub>** and point **P** with **{u<sub>x</sub>,u<sub>y</sub>,u<sub>z</sub>}**. In this case the program finds the distance, the perpendicular point **x<sub>0</sub>** and the reflected point **P'**.

### **EXAMPLE 1:**

Given are the lines **L<sub>1</sub>: {3,4,6} +  $\lambda \cdot \{-4,-6,-2\}$**  and **L<sub>2</sub>: {3,7,-2} +  $\mu \cdot \{2,8,-4\}$** .

Press **prgm** and select **EXEC** LINES. Press enter enter . The screen displays:

LINE 1: S+  $\lambda \cdot T$

S: Key in **{3,4,6}** enter. **Be sure to start each entry with a brace { ( the closing-brace } may be omitted ) and to enter a negative value with the (-) - key !.**

Continue:

T: **{-4,-6,-2}** enter

LINE 2: U+  $\mu \cdot V$

IF V={0,0,0}:

POINT P {UX,UY,UZ}

U: **{3,7,-2}** enter

V: **{2,8,-4}** enter

The result is:

DISTANCE = 2.0412414 ( ----- stored in variable **H** )

**The program pauses here**, press enter to continue:

P1 = {-6/5,-23/10,39/10} ( ----- stored in list **LP** )

P2 = {7/15,-47/15,46/15} ( ----- stored in list **LQ** )

$\alpha^\circ = 134^\circ 24' 55.111'' = 134.4153086$

### **EXAMPLE 2:**

Given L1: **{1,1,0} +  $\lambda \cdot \{-1,2,-1\}$**  and point P: **{1,2,3}**. Find the distance, point of perpendicular **x<sub>0</sub>** and reflected point.

Press **prgm** , then select **EXEC** LINES and press enter, enter. Then make the following inputs:

S: **{1,1,0}** enter

T: **{-1,2,-1}** enter

LINE 2: U+  $\mu \cdot V$

IF V={0,0,0}:

POINT P {UX,UY,UZ}

U: **{1,2,3}** enter

V: **{0,0,0}** enter (---- defines the last input as point! )

Result:

DISTANCE: 3.13581

PERPENDICULAR **x<sub>0</sub>**: {7/6 , 2/3 , 1/6} ( ----- stored in list **LP** )

REFLECTED POINT: {4/3 , -2/3 , -8/3 ( --- mirror-image point, stored in list **LS** ) !

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